EEE2035F: Signals and Systems I

Class Test 1

11 March 2011

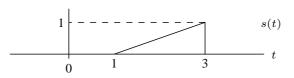
Name:

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Information

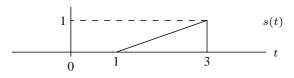
- The test is closed-book.
- This test has *four* questions, totalling 25 marks.
- Answer *all* the questions.
- You have 45 minutes.

1. (10 marks) Plot the signals given below. Where appropriate, assume that s(t) is the signal



- (a) $x_1(t) = \cos(\pi t)$.
- (b) $x_2(t) = \cos(\pi t)u(t+1)$.
- (c) $x_3(t) = \frac{d}{dt}s(t)$ (the generalised derivative).
- (d) $x_4(t) = \int_{-\infty}^t s(\lambda) d\lambda.$
- (e) $x_5(t) = s(3-t)$.

2. (5 marks) Let s(t) be the signal



and suppose that $y(t) = \delta(t) - \delta(t-2)$.

- (a) Plot y(t).
- (b) Calculate $\int_{-\infty}^{\infty} s(t)y(t)dt$.
- (c) Find $z(t) = \int_{-\infty}^{\infty} s(\lambda)y(t-\lambda)d\lambda$.

3. (5 marks) Let x(t) = u(t-2) and h(t) = u(t-1), where u(t) is the unit step

$$u(t) = \begin{cases} 1 & (t \ge 0) \\ 0 & (t < 0). \end{cases}$$

- (a) Plot x(t) and h(t).
- (b) Find and plot y(t) = x(t) * h(t).

4. (5 marks) Suppose we have a system

$$x(t)$$
 \longrightarrow H $y(t)$

that obeys the input-output relationship y(t) = x(t) + 1.

- (a) Find and plot the output $y_1(t)$ when the input is $x_1(t) = u(t)$.
- (b) Find and plot the output $y_2(t)$ when the input is $x_2(t) = 2u(t)$.
- (c) Is the system homogeneous?
- (d) Is the system linear?